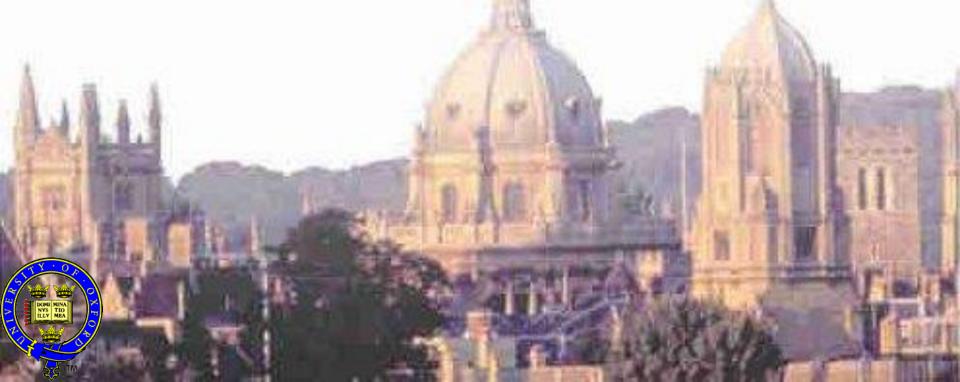
The continuing quest for quantitative image analysis

Sir Michael Brady FRS FREng FMedSci Professor of Oncological Imaging Department of Oncology University of Oxford



Overview

- Introduction: Medical imaging & Computer vision
- Breast cancer
 - Quantitative mammography + analytics, dose
 - Breast MRI
- Measuring therapy response
 - Colorectal cancer
- What cures cancer?
 - A cautionary tale: melanoma
 - Angiogenesis
- Another cautionary tale about quantitation
 - Shape and size of liver tumours

Medical Computer vision
Image ≠ +
Analysis clinical data

Medical image analysis addresses a specific medical problem:

- Working with clinicians
- What clinicians need
- What clinicians use
- The fundamental roles of models

Working with clinicians



Doctors specify the problem

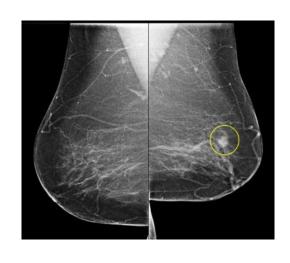


$$E^{\text{imp}}(\mathbf{x}) = \phi(V_t, \mathbf{x}) A_p t_s$$

$$\int_{0}^{E_{\text{max}}} N_0^{\text{rel}}(V_t, \varepsilon) G(\varepsilon) D(\varepsilon)$$

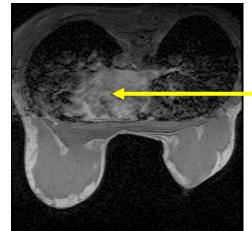
$$\exp^{-\mu_{\text{lucite}}(\varepsilon)h_{\text{plate}}} \exp^{-h\mu(\varepsilon)} d\varepsilon$$

Doctors are unimpressed by mathematics, algorithm details,



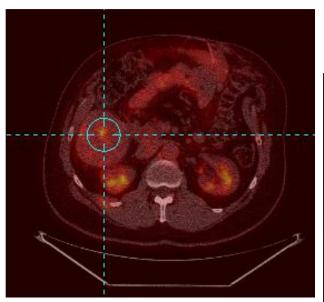
Doctors are impressed by results that enable them to work better

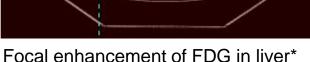
Confidence builds slowly, but can drop like a stone

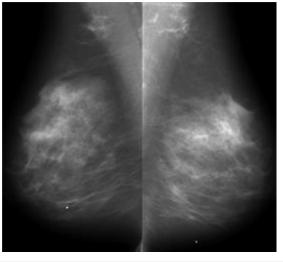


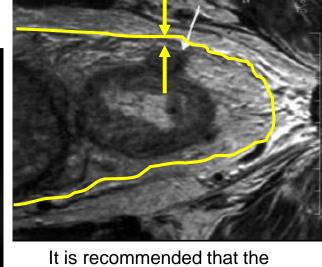
Algorithm: "this is a rapidly enhancing region, suggestive of cancer

What clinicians need









circumferential resection margin be at least 1mm if surgery is to be an option

in the same of the	1.5 mGy	~	9.1 kPa	V1.5.9	19	9.8%		
	Volumetric Bre		20	19.1				
1	Volume of Brea		631		645.5			
	Volume of Fibr	onlandular	Rig 129	Left 123.3				

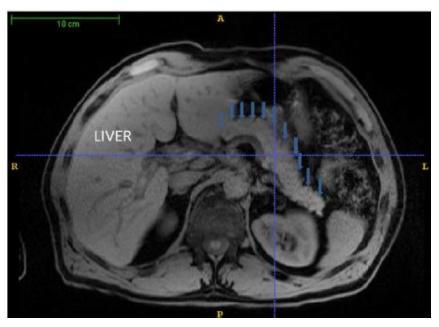
Tools they can trust & provide the information they need

Numbers!!!

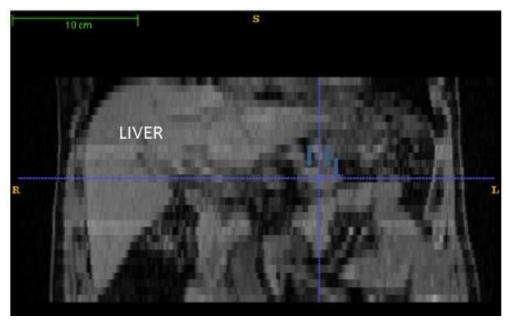
Accuracy

Response to therapy: If error in measurement m_i is ε_i , then error $(m_1 - m_2) = \varepsilon_1 + \varepsilon_2$

Image quality



Axial view of liver and pancreas (blue arrows)



Coronal view of the liver

Poor SNR compared to vision cameras, subject to artefact (e.g. bias field)

Poor sampling density:

- Partial volume effect
- Volume estimation and segmentation
- Interpolation? (Friday)
- Probability density function? (Friday)

The need to deliver accurate results, 24/7, 99.9% of the time, with poor SNR and sampling, massive variations across the normal population ... → incorporate models

Clinical aspects of Cancer

Breast cancer

- Breast density
- Microcalcifications
- Stellate masses

Colorectal cancer

- > circumferential resection margin
- > lymph node analysis
- > dceMRI & pharmacokinetic modeling

Liver cancer

- bias correction
- >breath hold
- > time to enhancement
- > morphology to aggressive mutation



Biological aspects of Cancer

Angiogenesis

- Compartment model
- angiogenic switch

Glycolysis

- > quiescence
- > pH control

Hypoxia

- vascularity
- AKT/PTEN modulation of HIF
- > relation to PET imaging

Image analysis methods

Feature detection

- > Phase congruency
- Monogenic signal
- > scale-saliency

Deformable registration

- Physiological constraints
- Probability density estimation
 - ➤ Non-Parametric Windows
- Level sets
 - > Bhattacharya flow





Models of image formation



• (x-ray) Mammography

- > X-ray attenuation, Beer's law
- ➤ Scatter

MRI

- > T1 estimation
- bias correction
- contrast enhancement & pharmacokinetics
- >pharmacokinetic modelling

PET/SPECT

- > radioligand
- ▶gated PET

Clinical aspects of Cancer

- Breast cancer
 - Breast density
 - Microcalcifications
 - Stellate masses
- Colorectal cancer
 - circumferential resection margin
 - > lymph node analysis
 - dceMRI & pharmacokinetic modeling
- Liver cancer
 - bias correction
 - >breath hold
 - > time to enhancement
 - > morphology to aggressive mutation



Biological aspects of Cancer

- Angiogenesis
 - Compartment model
 - angiogenic switch
- Glycolysis
 - > quiescence
 - > pH control
- Hypoxia
 - vascularity
 - > AKT/PTEN modulation of HIF
 - > relation to PET imaging

Image analysis methods

- Feature detection
 - Phase congruency
 - Monogenic signal
 - > scale-saliency
- Deformable registration
 - Physiological constraints
- Probability density estimation
 - Non-Parametric Windows
- Level sets
 - > Bhattacharya flow





Models of image formation



- (x-ray) Mammography
 - > X-ray attenuation, Beer's law
 - > Scatter
- MRI
 - > T1 estimation
 - bias correction
 - contrast enhancement & pharmacokinetics
 - pharmacokinetic modelling
- PET/SPECT
 - > radioligand
 - ▶gated PET

Cancer in Europe 2012

New cases: 3.45M, deaths: 1.75M

Cases

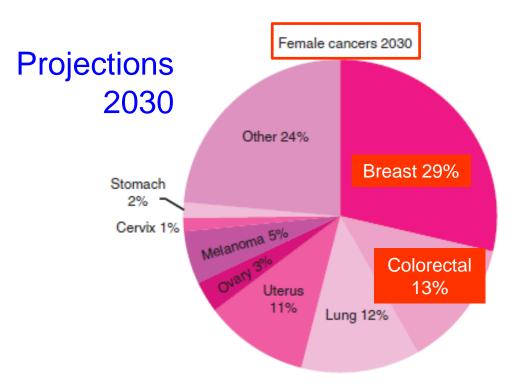
– Breast : 474,000 (deaths: 131,000)

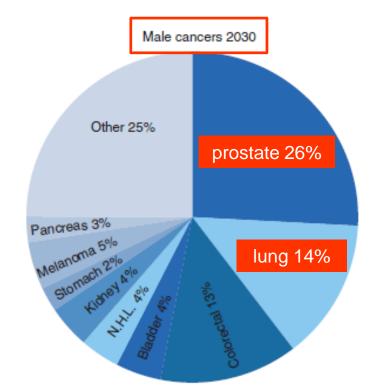
Colorectal: 447,000 (deaths: 215,000)

Lung: 411,000 (deaths: 353,000)

UK lifetime risk of getting cancer will be 47% by 2020 (44% in 2012)

By 2020, 38% will survive cancer to die of another cause (35% in 2012)





How many different kinds of cancer are there?

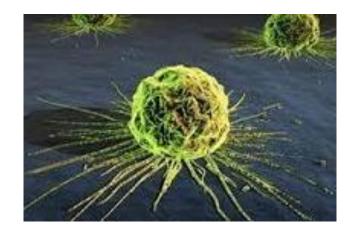
Until 20th Century: 1

1990: over 100

Today:

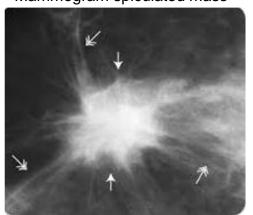
"There are more than 200 different types of cancer. You can develop cancer in any body organ. There are over 60 different organs in the body where a cancer can develop. Each organ is made up of several different types of cells."

> The word "cancer" was apparently first coined by Hippocratus, 1500BCE, because of the resemblance of the shape to a crab..



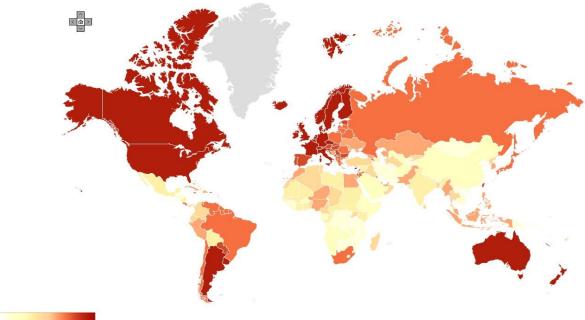


Mammogram spiculated mass



Breast cancer incidence

▲ Estimated Breast Cancer Incidence Worldwide in 2008

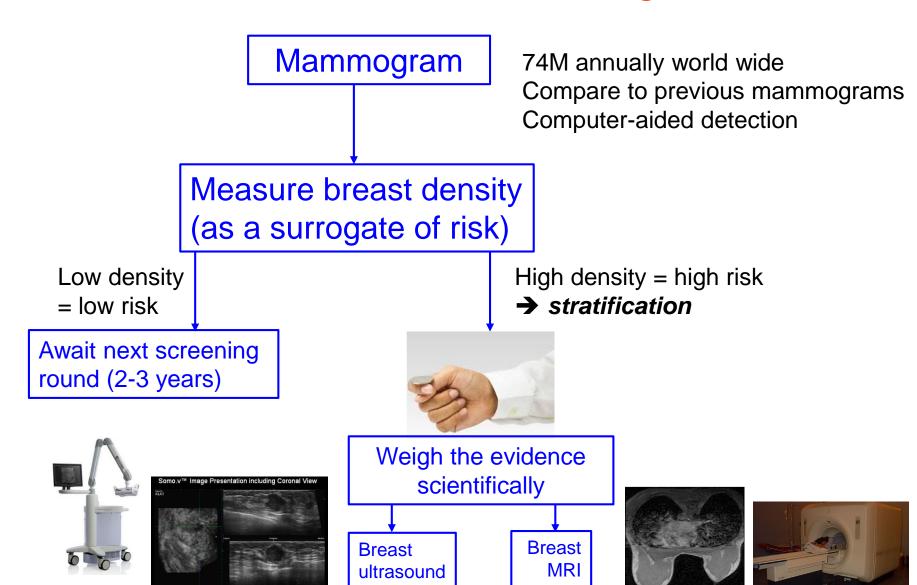


- 0 18.9 27.2 40.0 64.0 110 Age-standardised incidence rates per 100,000
- In developed countries, 1 in 8 women will get breast cancer at some point
- 23% of all cancers in women projected to rise to 29% by 2030
- Peak incidence is women over 60

- In developing countries, including BRIC, numbers are rising rapidly, already 500,000 cases in 2008
- Reasons: increasing urbanisation, changes in lifestyle
- Impacting particularly on younger women

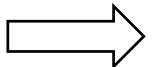
Early detection + chemo/radio/conservative surgery + risk analysis is transforming morbidity

Personalised screening



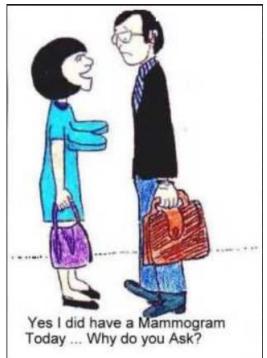


Mammogram









Breast density

- Mammography is only 48% effective in dense breasts, compared to 98% in fatty breasts
- 40% of women have dense breasts, postmenopausal, i.e. involution ineffective
- Breast density is a more significant risk factor than having a mother and sister with breast cancer
- Cancer recurrence is four times more likely in women with dense breasts
- Perfect storm ...
- BIRADS: the result of years of discussion by the American College of Radiology

Current Breast Density Classifications

BI-RADS®: The American College of Radiology (ACR) has published a set of criteria which radiologist's use to categorize their opinion of the absence or likelihood of disease. Within that criteria is also a visually-assessed BI-RADS breast density category (an area-based breast density assessment method). Those categories are:

Category 1 — The breast is almost entirely fat (<25% glandular).

Category 2 — There are scattered fibroglandular densities (approximately 25-50% glandular).

Category 3 — The breast tissue is heterogeneously dense, which could obscure detection of small masses (approximately 51% – 75% glandular).

Category 4 — The breast tissue is extremely dense. This may lower the sensitivity of mammography (>76% glandular).

These are commonly called the BI-RADS breast composition categories. Radiologists in the US should record every woman's breast density using the BI-RADS scheme.



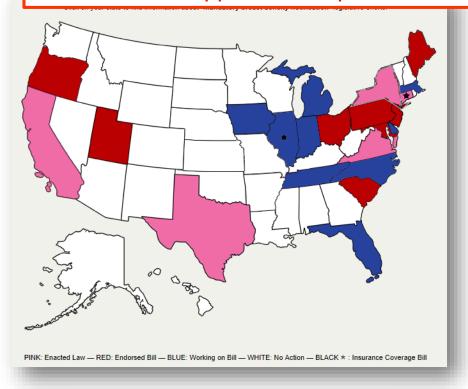
BIRADS = cloud classification

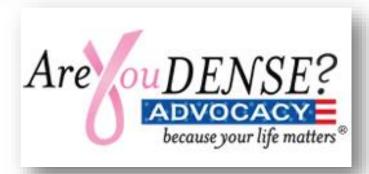


Surely, we can do better? Remember that we want numbers!

Breast Density Legislation

This is welcomed by women; but what are clinicians supposed to report??





AMENDED IN SENATE MARCH 27, 2012

SENATE BILL

No. 1538

Introduced by Senator Simitian (Principal coauthors: Senators Alquist and Runner)

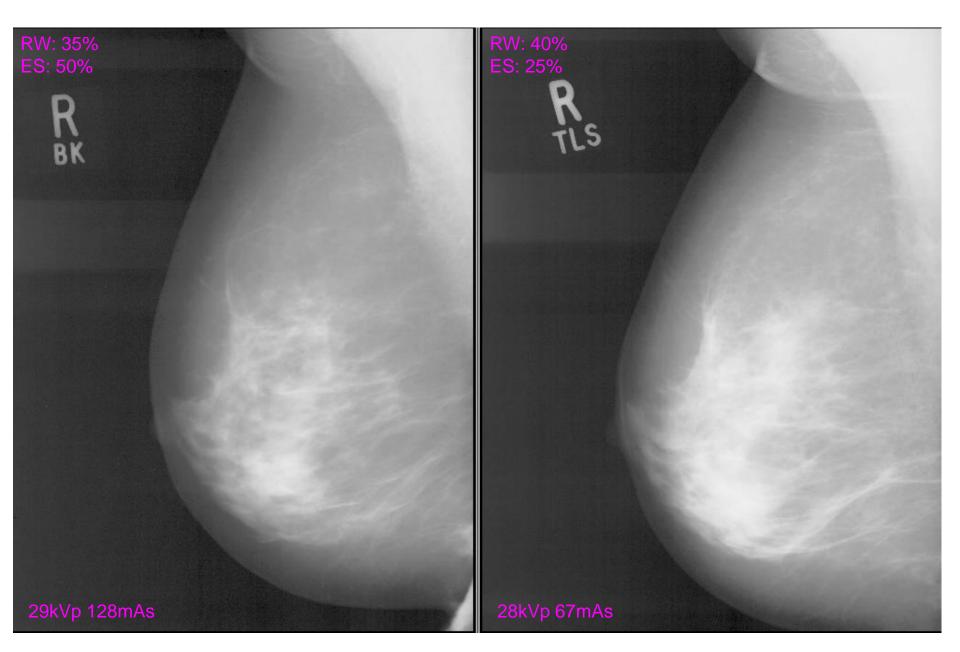
A BILL

To require breast density reporting to physicians and patients by facilities that perform mammograms, and for other purposes.

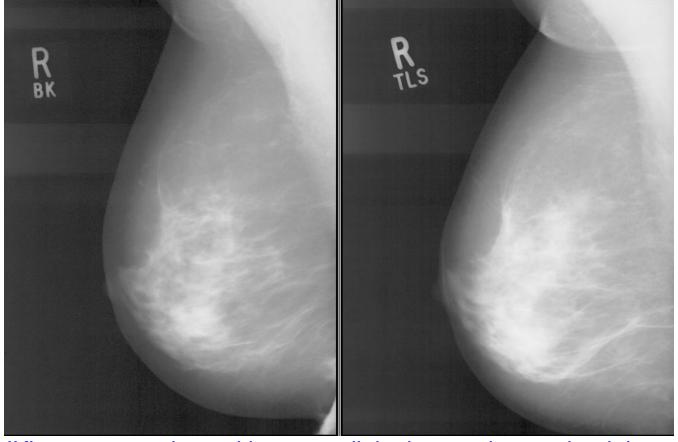
- 1 Be it enacted by the Senate and House of Representa-
- 2 tives of the United States of America in Congress assembled,
- 3 SECTION 1. SHORT TITLE.
- 4 This Act may be cited as the "Breast Density and
- 5 Mammography Reporting Act of 2014".



Mammography: Image Parameter Dependence



Estimating breast density



Two of the UK's most experienced breast radiologists each examined the two mammograms shown, to estimate the percentage of dense tissue.

BK estimated 25%; TLS estimated 40% but it is the same breast!!!

Why is that?

Answer: the left image was exposed to x-rays twice as much as the right





In photography, we exploit exposure time, F-stop, "film speed", ... to create a range of effects, and to highlight things that we are interested in...

First technological capability: need for quantitative analysis in mammography

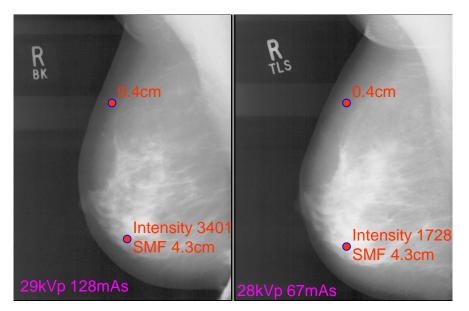


Image intensity relates to anatomy in a very complex way image analysis a hard problem.

Starting 1994, with Ralph Highnam, I have invented a sequence or solutions to this problem:

- h_{int}(x) a quantitative representation of the image assigning to each pixel x the amount of non-fat (interesting) tissue at that pixel location x;
- Volpara density a fast, relative physics model developed by Matakina Ltd

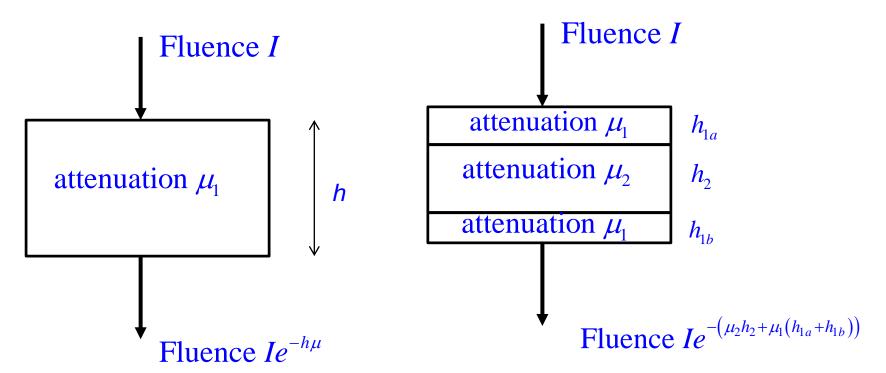
COMPUTATIONAL IMAGING AND VISION

Mammographic

Image Analysis

Aichael Brady

First, a tiny bit of physics: Beer's Law



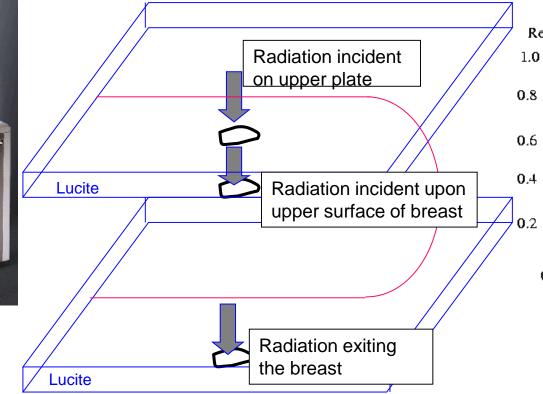
Note that the exiting fluence is the same irrespective of where, vertically, the block of attenuation μ_2 is.

Mammography is fundamentally projective: though digital breast tomosynthesis is changing that...

A model of mammographic image formation



↓ indicates photon fluence



Relative photon output

..0

..0

..0

..8

..6

..4

..2

Photon energy (keV)

Output of a typical

Output of a typical mammography x-ray tube

Energy that reaches the imaging sensor:

$$E^{\text{imp}}(\mathbf{x}) = \phi(V_t, \mathbf{x}) A_p t_s \int_{0}^{E_{\text{max}}} T(\varepsilon) \exp^{-\mu_{\text{lucite}}(\varepsilon) h_{\text{plate}}} \exp^{-h\mu(\varepsilon)} d\varepsilon$$

 $\phi(V_t, \mathbf{x})$ = tube voltage t_s = exposure time A_p = pixel size

where $T(\varepsilon)$ is the transfer function (spectrum energy, image gain,)

Highnam & Brady's h_{int} model

The literature tells us* that you cannot distinguish stromal tissue and tumours on the basis of their x-ray attenuations \rightarrow two kinds of tissue: *fat* & *"interesting"*. If the compression between the plates is H cm, then at any given pixel \mathbf{x} , we have $H = h_{\text{fat}}(\mathbf{x}) + h_{\text{int}}(\mathbf{x})$

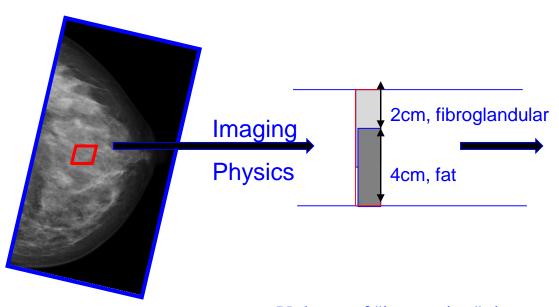
Our job is to find $h_{int}(\mathbf{x})$ for every voxel \mathbf{x} . We know H and the tube parameters.

What can we find from the equation of photon fluence?:

$$E^{\mathrm{imp}}(\mathbf{x}) = \phi(V_t, \mathbf{x}) A_p t_s \int_0^{E_{\mathrm{max}}} T(\varepsilon) \exp^{-\mu_{\mathrm{lucite}}(\varepsilon)h_{\mathrm{plate}}} \exp^{-h\mu(\varepsilon)} d\varepsilon$$
We measure this We know all this stuff Compression plates – we don't know! know that too
$$h\mu(\varepsilon) = h_{\mathrm{int}} \mu_{\mathrm{int}}(\varepsilon) + h_{\mathrm{fat}} \mu_{\mathrm{fat}}(\varepsilon)$$

$$= h_{\mathrm{int}}(\mu_{\mathrm{int}}(\varepsilon) - \mu_{\mathrm{fat}}(\varepsilon)) + H \mu_{\mathrm{fat}}(\varepsilon)$$

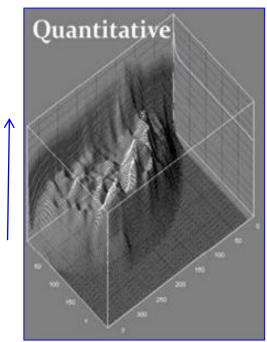
Volume-based Density Measurement



Volumetric Breast Density =

Volume of "interesting" tissue

Volume of the breast



cm



"Relative physics"

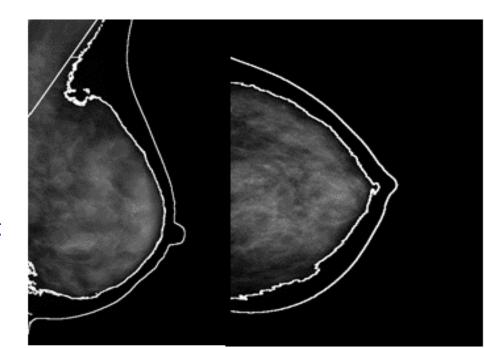
Highnam, Brady, Karssemeijer, and Yaffe

We have to know all those calibration parameters for Highnam and Brady's method to work. We can guess at lots of them.. BUT

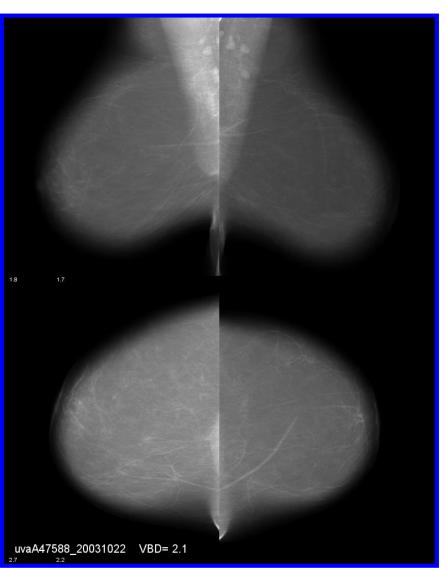
Suppose we knew a region of the breast that was *entirely fat...* We could then use this as a "reference"

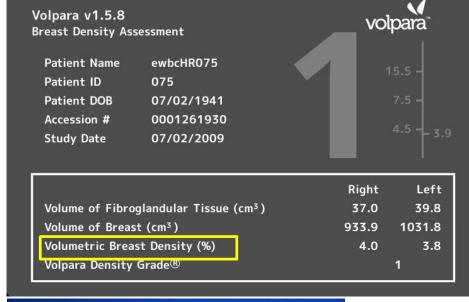
$$h_{\rm d}(\mathbf{x}) = \frac{\ln\left(I_{\rm obs}(\mathbf{x})/I_{\rm fat}\right)}{\mu_{\rm fat} - \mu_{\rm dense}}$$

We need accurate breast inner/outer boundary segmentation We use phase congruency



Volume-based Methods for Density Measurement

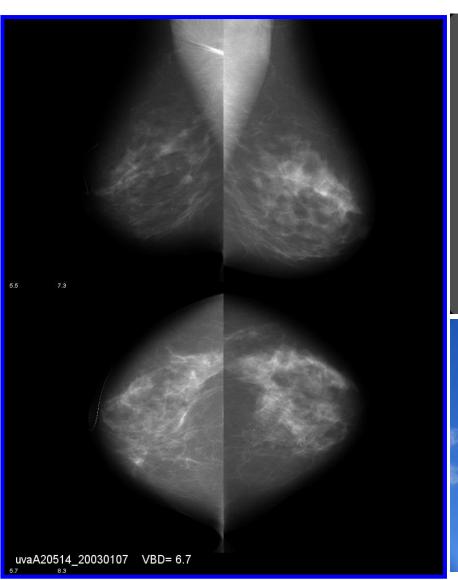


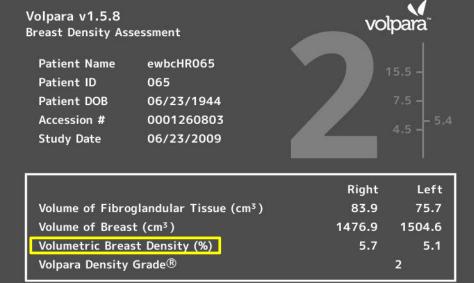


Sky analogy



Volume-based Methods for Density Measurement



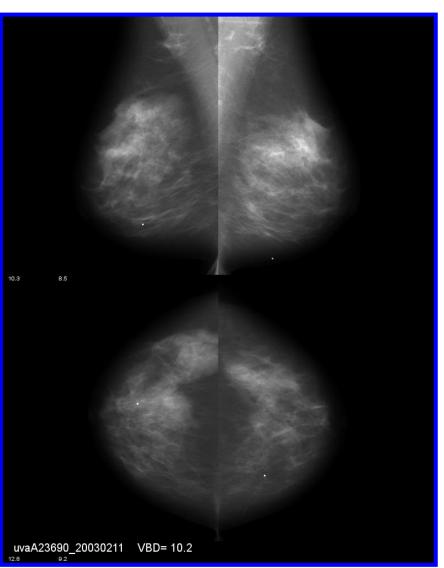


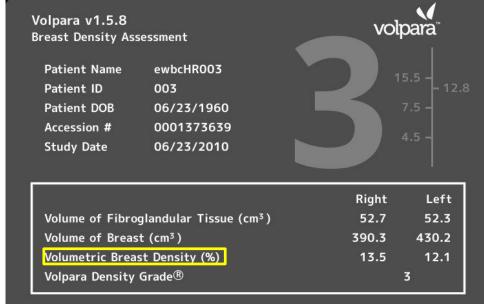


Sky analogy



Volume-based Methods for Density Measurement



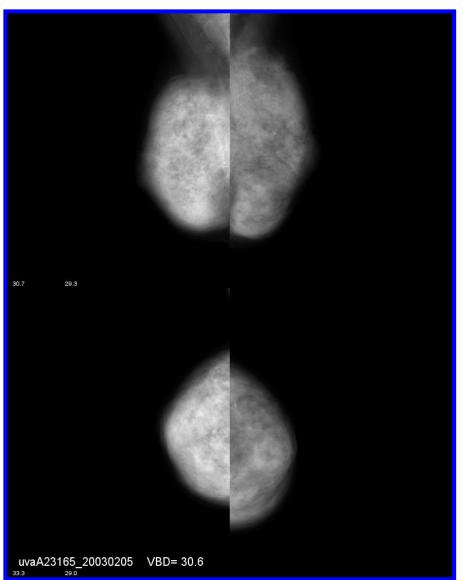


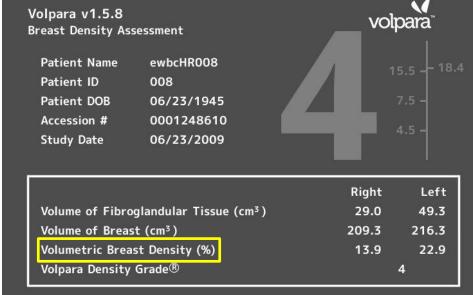


Sky analogy



Volume-based methods for density measurement









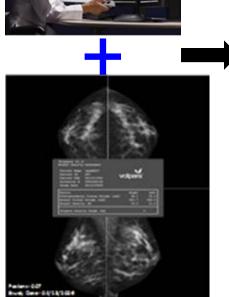


Patient stratification



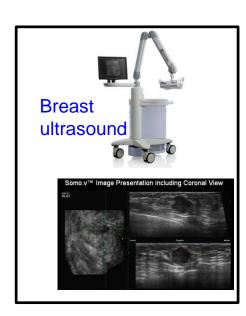
Woman has a mammo

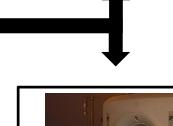
Volpara breast density score immediately available

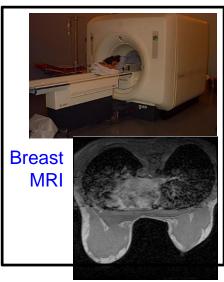




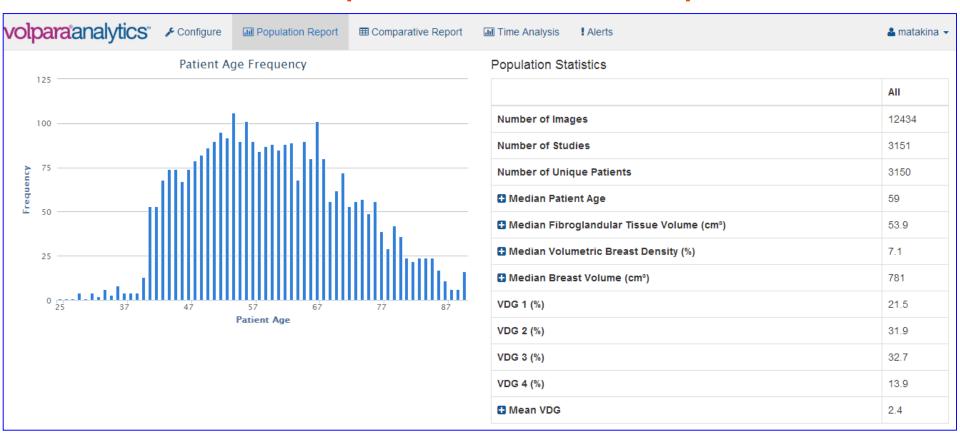
Woman can decide on supplementary screening before she leaves clinic.





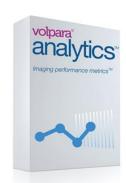


Numbers provide statistical power

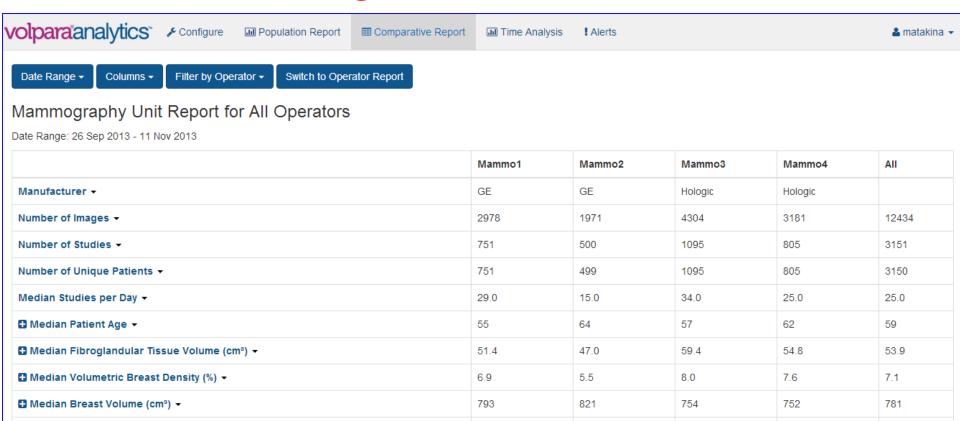


Remember:

- 74 million mammograms per year
- Density varies with population
- There may be genetic involvement beyond HER-2
- Analysis lends itself to cloud delivery



Management Information



Most large screening centres have multiple mammography units

- They vary by manufacturer, model, and vintage
- They may show variable results but is this due to the population screened using that machine or due to the machine itself?



Quality control

volpara*
analytics*
Imaging performance metrics**

Automated quality control of mammography machines, radiographers, population usage ... all this needs statistical power to be meaningful



	1	2	3	4	5	6	7	8	9	10 1	1 1 A	All
Number of Images		316	270	254	214	209	195	173	148	113	68	18364
Number of Studies		81	69	64	54	53	50	44	37	30	18	4680
Number of Unique Women	81	81	69	64	53	53	50	44	37	30	17	4656
Median Age	55	56	60	59	57	55	59	59	55	51	59	58
Median Volumetric Breast Density (%)	6.7	6.8	6.9	8.5	6.2	7.0	7.6	6.8	7.3	6.1	7.8	7.0
Median Fibroglandular Tissue Volume (cm³)	55.0	52.7	53.2	52.3	51.1	53.5	53.9	53.4	62.2	45.1	58.5	54.0
Median Breast Volume (cm³)	810	876	798	623	773	758	713	851	821	754	791	772
Median Breast Thickness (mm)	62	62	60	53	62	61	58	59	61	62	63	60
Median Compression Force (N)	75	98	66	98	73	79	83	108	73	70	58	80
Median Contact Area (mm²)	9993	8570	7754	7515	9059	8103	7256	9064	7348	6652	7982	7993
Median Pressure Applied (kPa)	8.3	11.4	7.9	12.1	7.6	10.1	9.9	12.6	8.9	10.3	6.4	9.8

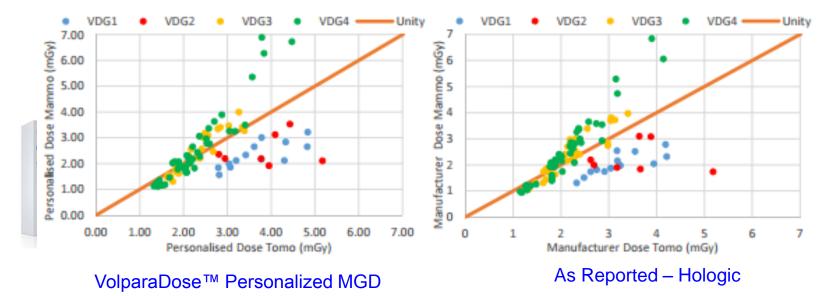
This provides usage statistics on individual radiographers (technologists in US parlance)

Operator 11 may need re-training....



mātakina international™

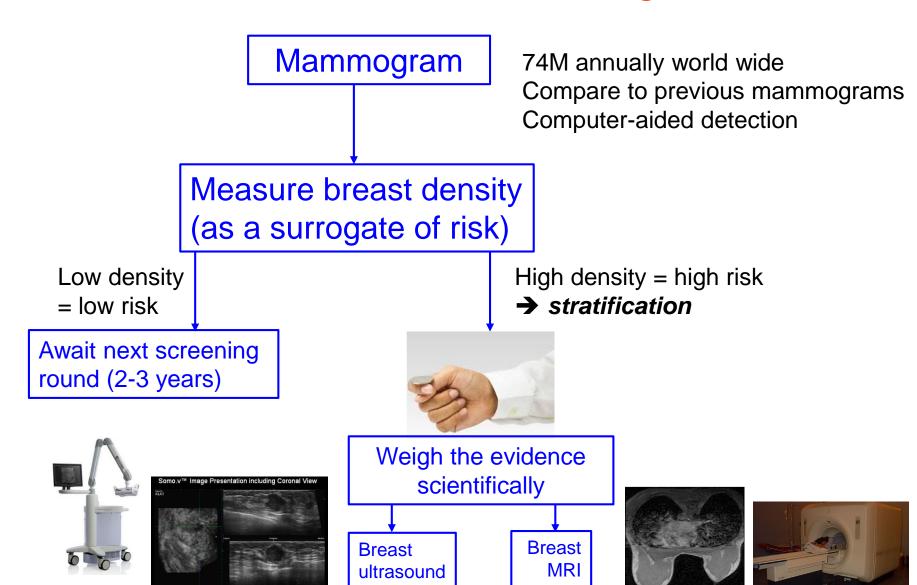
Personalising x-ray dose calculation



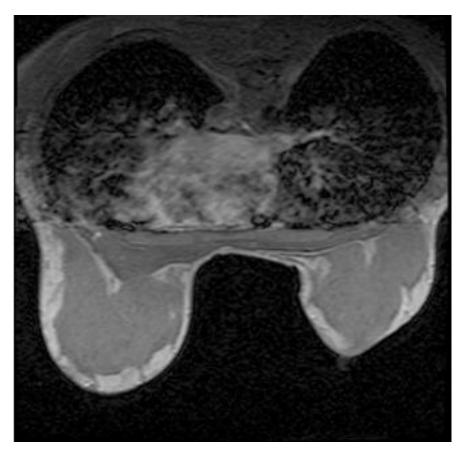
- X-ray dose is low in mammography, but
 - Millions of women per year X minimal risk of excessive dose per woman = likelihood of x-ray induced cancer each year
- FDA MQSA requirements are that the mean glandular dose is under 3mGy for specific phantoms
 - Women are not phantoms!
- Each manufacturer shows mean glandular dose (MGD) for each image, but
 - Each manufacturer uses a different algorithm to estimate MGD
 - Comparison machine/machine and model/model is nigh impossible
 - Records of accumulated dose become highly suspect
- Calculate it using our mathematical model + DICOM header information



Personalised screening



Breast MRI uses contrast agent





No abnormal tissue visible

Contrast Agent Uptake Profiles

Malignant to benign distinction is improved using concentration based analysis.

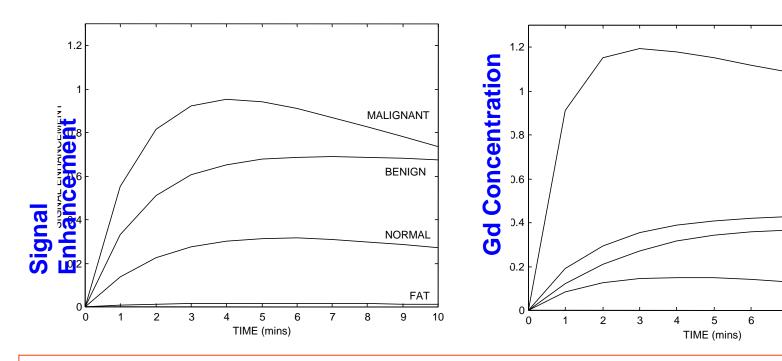
MALIGNANT

BENIGN

NORMAL

FAT

10



Gd concentration is proportional to the change ΔT_1 so we need first to **measure T_1**

Measuring T₁

For a MRI gradient echo pulse sequence, one can derive a signal model:

$$S = g\rho e^{-TE/T_2^*} \sin \alpha \frac{1 - e^{-TR/T_1}}{1 - \cos \alpha e^{-TR/T_1}}$$

Note that T_2^*, T_1 are of interest, fixed for any given voxel (but are not known); g, ρ depend on the particular machine, and are also unknown The only things we can vary are: α, TR, TE : in practice, vary α

Rearranging:
$$\left[\frac{S}{\sin \alpha} \right] = e^{-TR/T_1} \left[\frac{S}{\tan \alpha} \right] + g \rho e^{-TE/T_2^*} \left(1 - e^{-TR/T_1} \right)$$

$$y = mx + c$$

Fixing TR, TE and choosing a set $\{\alpha_i\}$, observing resulting $\{S_i\}$: estimation of $m = e^{-TR/T_1} \Rightarrow \hat{T}_1$

Contrast agent

Signal model

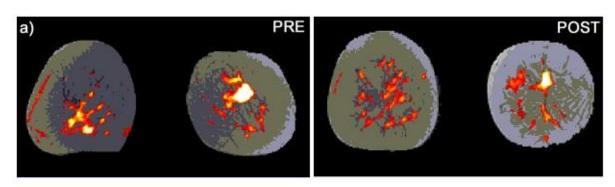
$$S = g\rho e^{-TE/T_2^*} \sin \alpha \frac{1 - e^{-TR/T_1}}{1 - \cos \alpha e^{-TR/T_1}}$$

Add effects of contrast agent (T₁ & T₂ alteration).

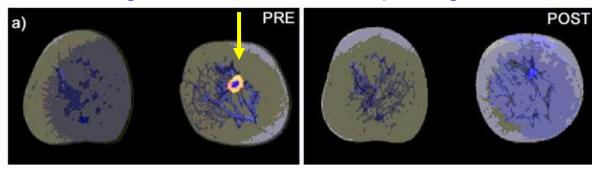
$$S(C_t) = g\rho e^{-TE\left(\frac{1}{T_2^*} + R_2C_t\right)} \sin\alpha \frac{1 - e^{-TR\left(\frac{1}{T_1} + R_1C_t\right)}}{1 - \cos\alpha e^{-TR\left(\frac{1}{T_1} + R_1C_t\right)}}$$

... there are numerous other methods for estimating T_1 and there are models for all other MRI pulse sequences, such as spin echo, ...

Measuring effect of chemotherapy



Pre- and post-chemotherapy
Percentage increase in intensity at right

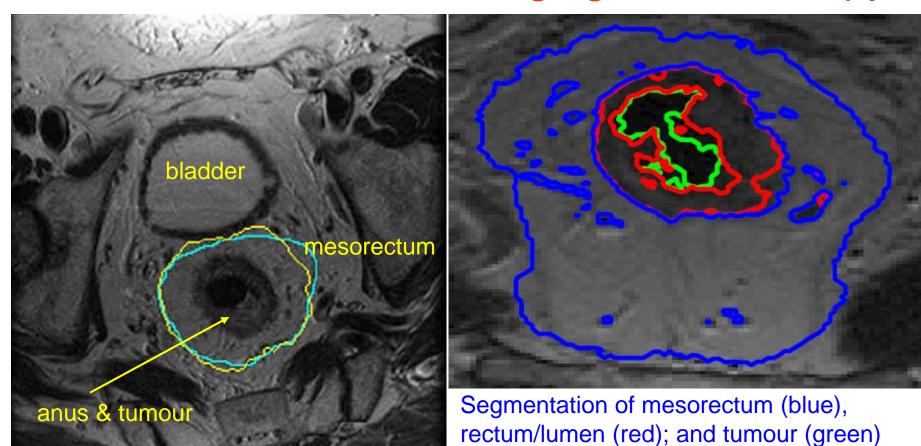


Pre- and post-chemotherapy ΔT_1 at left

(non-rigid) registration and pre- and post-chemotherapy, from ΔT1



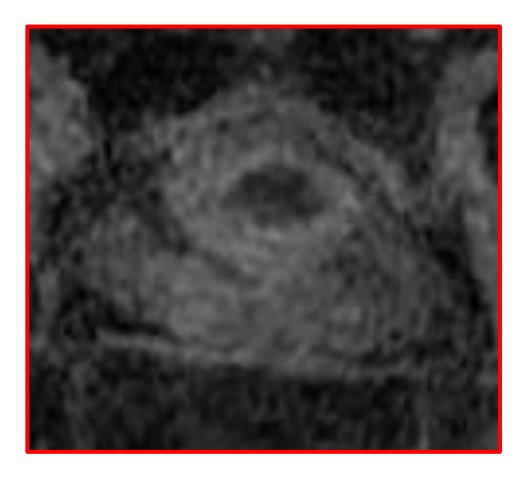
Colorectal cancer: downstaging chemotherapy



Most patients get down-staging chemotherapy prior to surgery 10% of patients who have surgery turn out to be complete responders to the chemotherapy; but still have the surgery (and the substantially negative impact on quality of life afterwards)

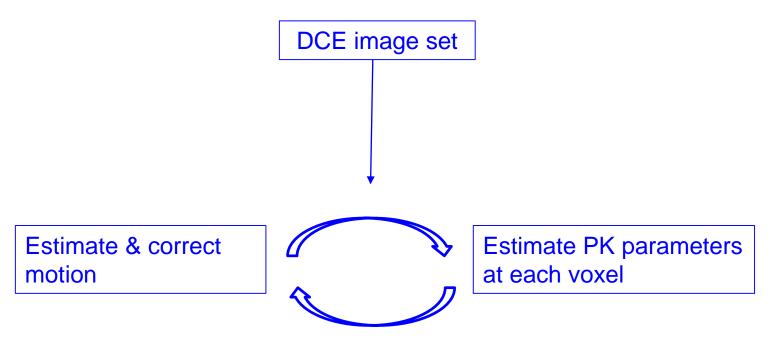
Can we tell who are most likely to be complete responders??

Colorectal cancer dceMRI: motion



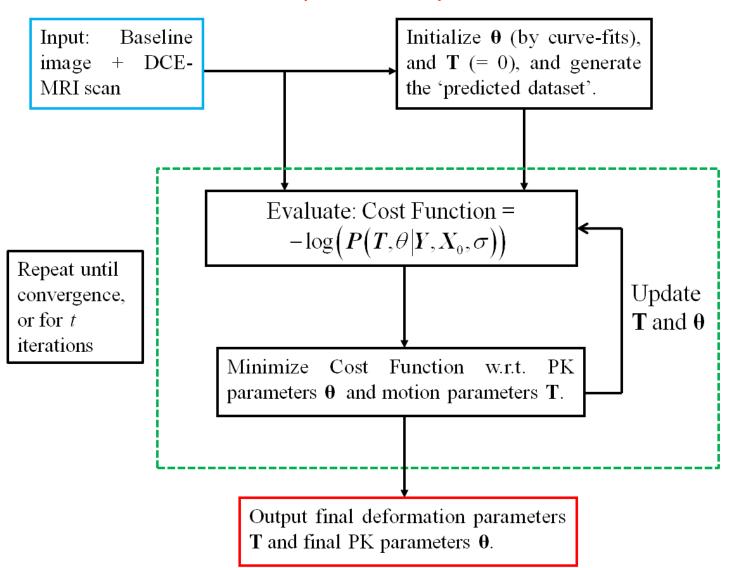
Original data

Simultaneous estimation of motion parameters and PK parameters

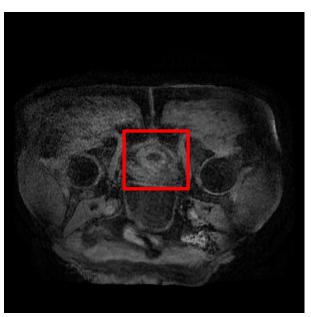


There are numerous ways in which this cycle can be developed mathematically and implemented in an efficient algorithm. The simplest is expectation-maximisation...though there are several others

Model-based Registration and Parameter Estimation (MoRPE)



Motion correction of dceMRI volumes for colorectal cancer



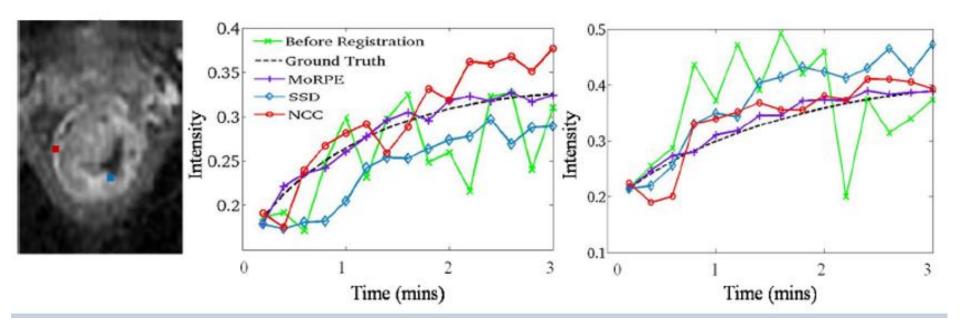




Original data

Motion corrected

Signal intensity curves

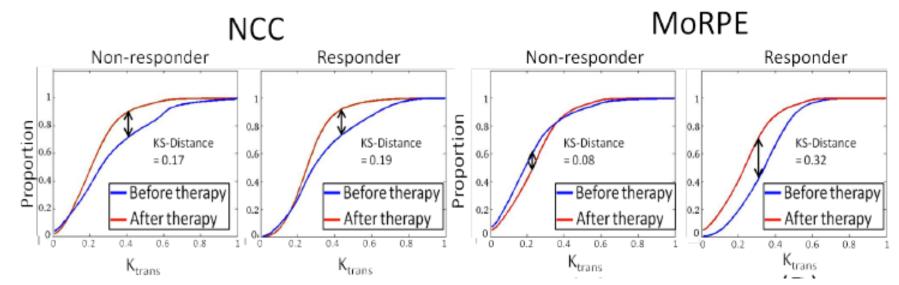


In this case, the signal change and motion were simulated. (----)
The simultaneous algorithm:

Two standard similarity criteria for deformable registration:



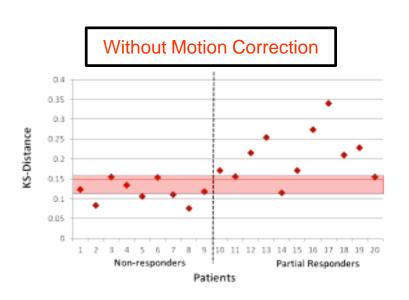
Measuring therapy response



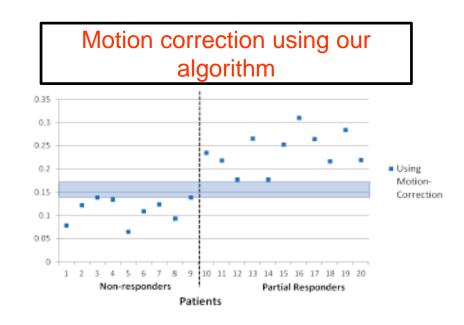
No discrimination for non-responder/ responder case using conventional normalised cross-correlation (NCC) registration Increase in perfusion for responder vs no change in non-responder case using MoRPE (PK model-based registration)

Motion correction: Differences in K_{trans} distributions before & after therapy

The importance of motion correction



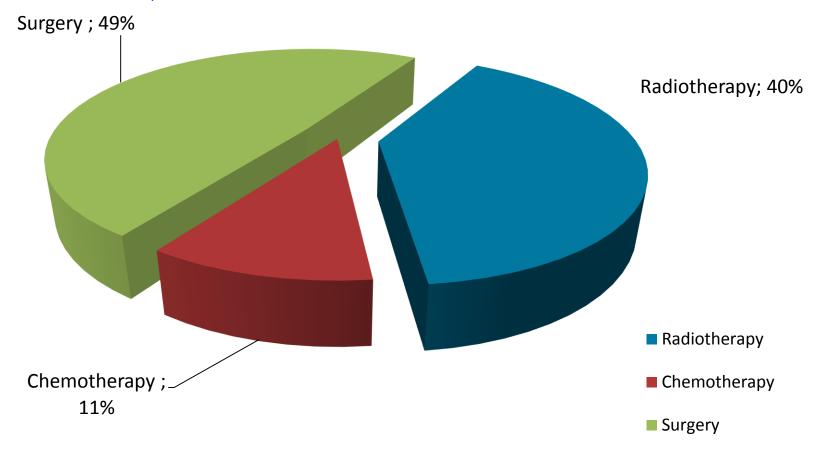
discrimination between responders & non-responders is not possible without motion correction



Statistically significant* discrimination between responders & non-responders

What can currently cure cancer?

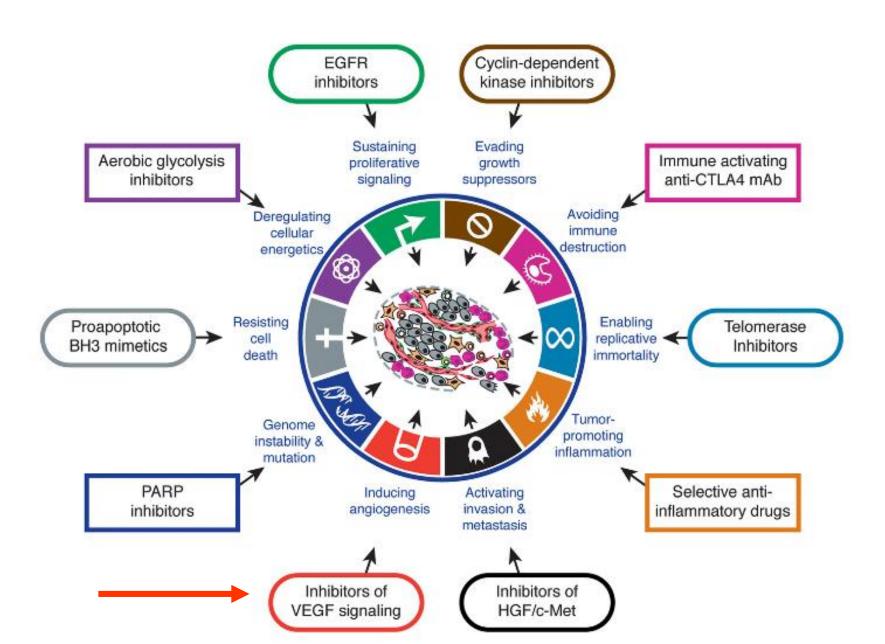
Professor Sir Mike Richards, NCRI 2011



Can we define biological processes that regulate or are markers of the responsiveness of tumours?

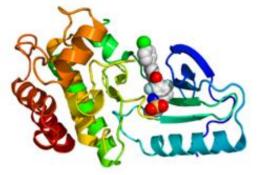
Can agents that target these processes be taken into the clinic to alter outcome?

Hanahan and Weinberg Hallmarks of Cancer

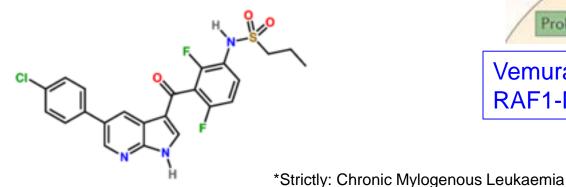


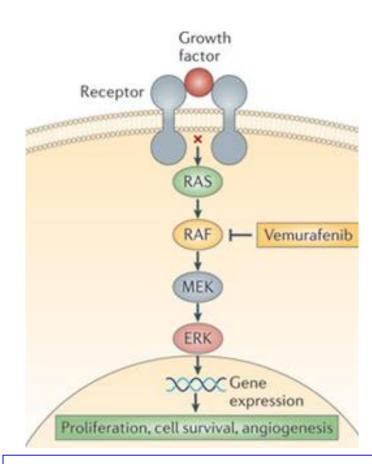
An early example: Melanoma*

40-60% of patients with melanoma have activating mutations of BRAF – a proto-oncogene that makes a protein B-RAF, which is involved in signalling in cells related to cell growth



PLX4032 (Vemurafenib) is an inhibitor of BRAF kinase



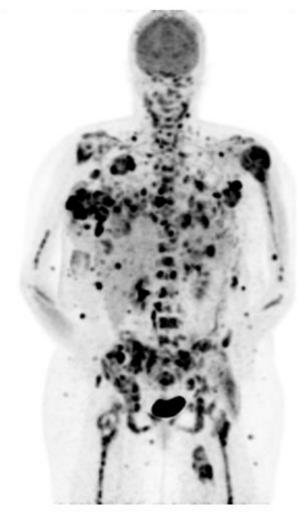


Vemurafenib targets the RAS-RAF1-MEK-ERK pathway

Image of a BRAF-mutant melanoma

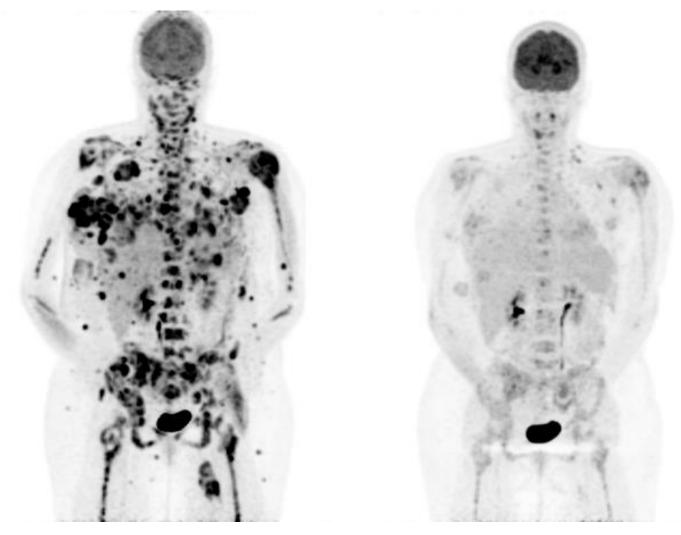


Man, 38 years old with a BRAFmutant melanoma



PET fluorodeoxyglucose (FDG) image

PET imaging shows the impact of Vemurafenib

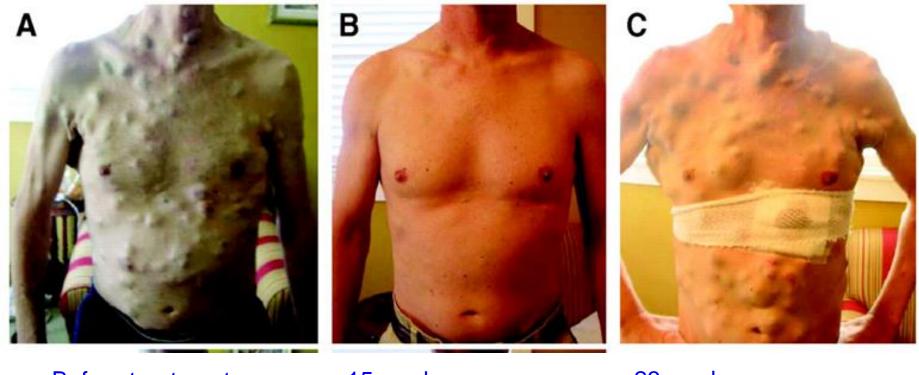


Before and two weeks after initiating PLX4032

"This is one of the best examples I've ever seen of science triumphing over disease." Brian Druker



...or so they thought



Before treatment

15 weeks...

23 weeks...

Conclusion

....cancer is agile.. It rapidly learns to mutate to accommodate a new therapy.....

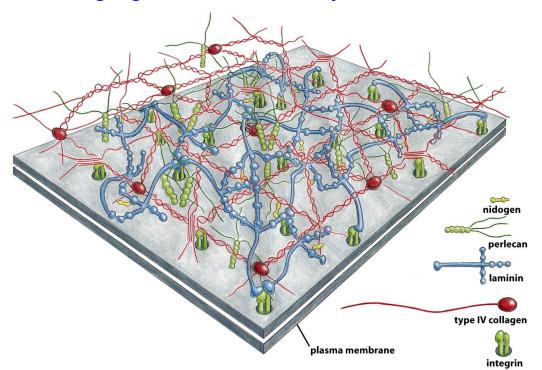
This is a salutary lesson ... but it is not all such bad news....

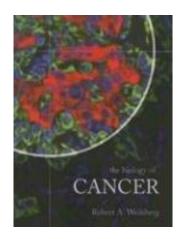
A bit of biology....

Cancers don't just develop as aberrant processes *within* a cell, rather by a complex series of interactions with the cells in their neighbourhood, that form the normal epithelia.

In normal tissue, these form the basement membrane

Tumour angiogenesis has many similarities to normal wound healing ...





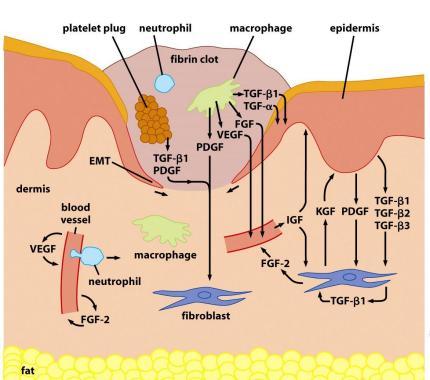
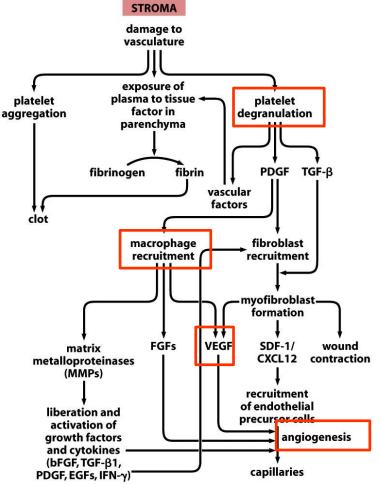


Figure 13-14 The Biology of Cancer (© Garland Science 2007)

Pathway model

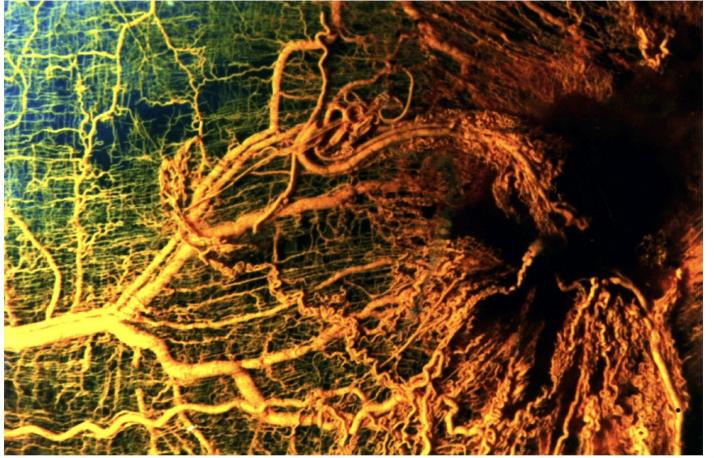
A picture of wound healing....



epithelial cells TGF-β1, MMPs from stroma morph into mesenchymal cells (EMT) move into wound site and cover wound morph into epithelial cells (MET) reconstruct epithelium

EPITHELIUM

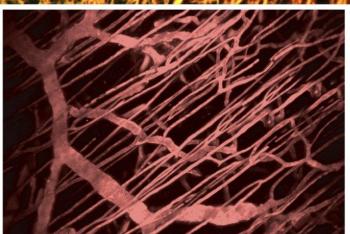
Figure 13-10 The Biology of Cancer (© Garland Science 2007)

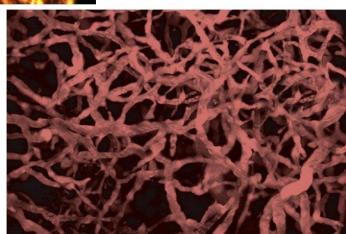


Above, left: normal; right chaotic (tumour is black)

Figure 13-34a The Biology of Cancer (© Garland Science 2

Another rendition of chaotic & leaky neovasculature

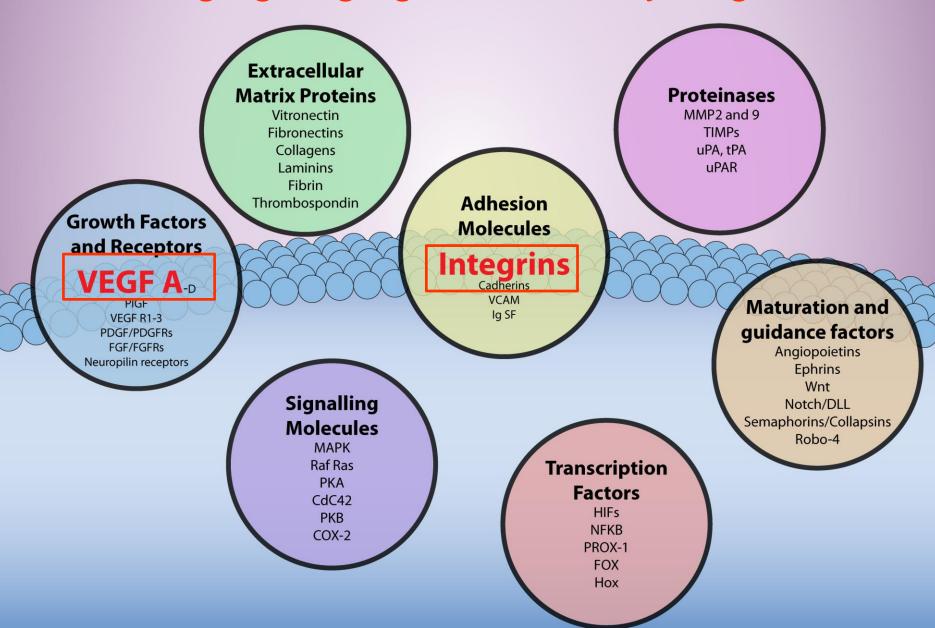




normal tissue

tumor

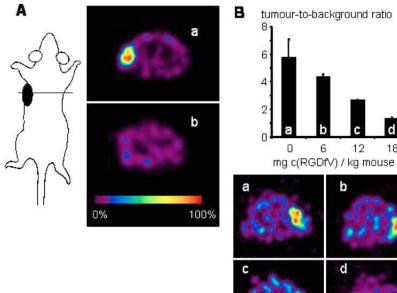
Imaging angiogenesis: many targets!



Integrin targeting for angiogenesis

Integrins 'integrate' signals from the extracellular matrix (ECM) to the intracellular cytoskeleton in focal adhesions.

In particular, the integrin $\alpha v \beta 3$ mediates the migration of endothelial cells through the basement membrane during blood-vessel formation. It binds to peptides containing the amino-acid sequence RGD*



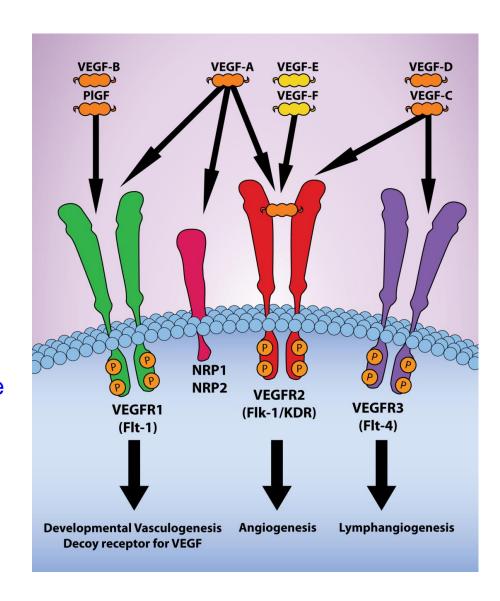
^{*} Arginine-Glycine-Aspartic acid

¹⁸F-RGD PET-CT image of small renal tumours

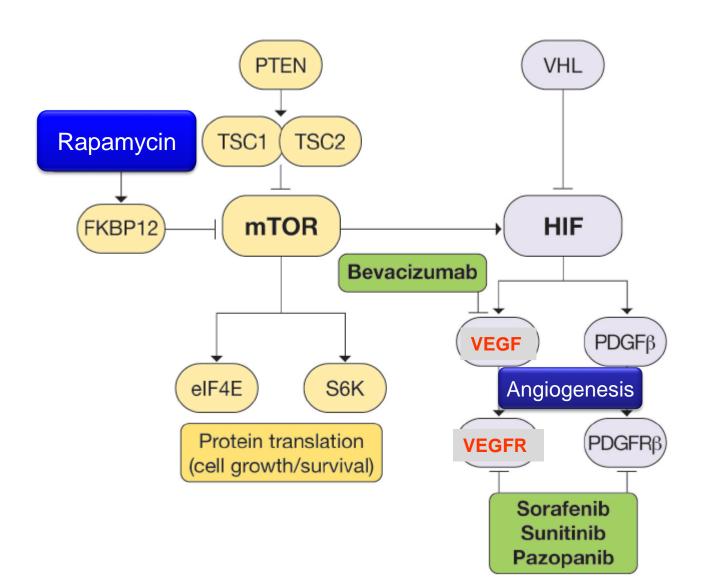
VEGF for inhibition of angiogenesis

Vascular Endothelial Growth Factors VEGF A-D are signalling proteins

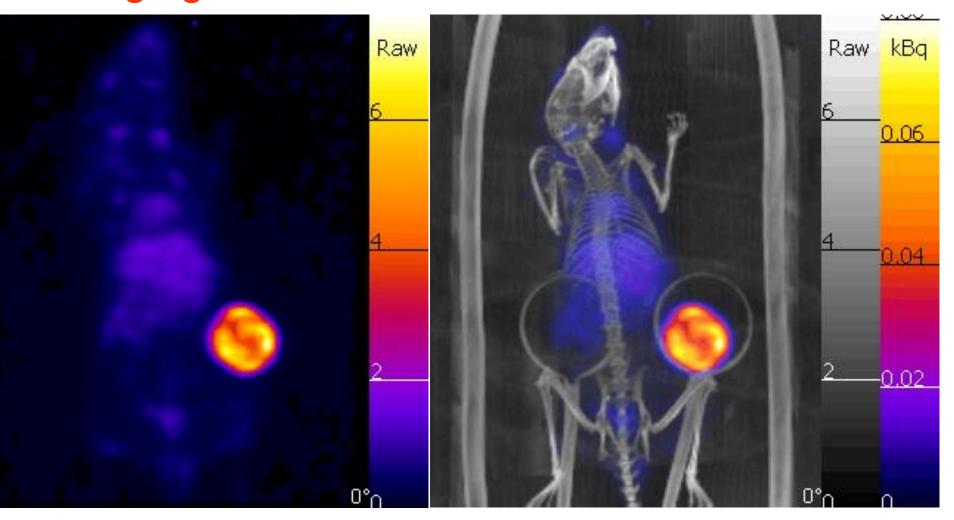
Cellular response through the tyrosine kinase receptors (the VEGFR 1-3) on the cell surface

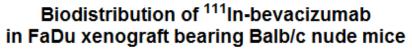


A range of related targets

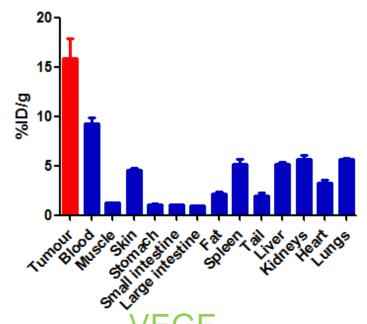


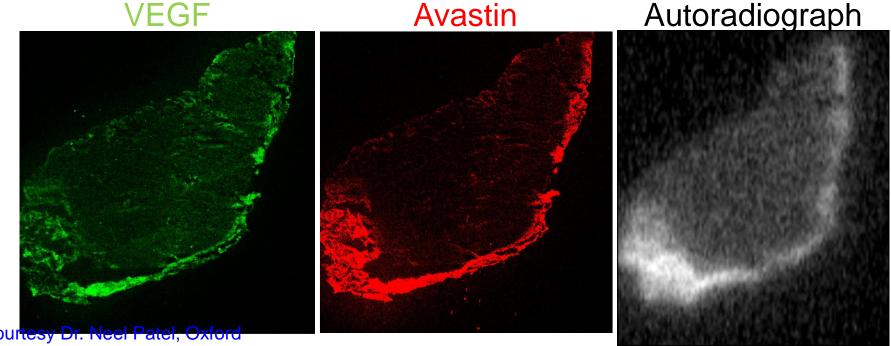
Imaging Avastin bound to SPECT emitter 124I





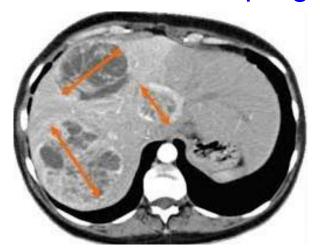
Biodistribution & immunohistochemistry





Finally, a cautionary tale about quantitation

How are tumour progression/response measured?



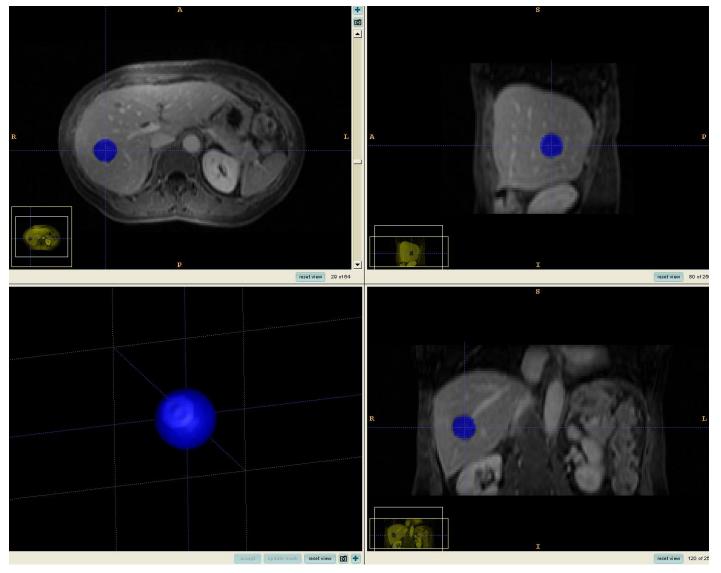
Response Evaluation Criteria in Solid Tumours (RECIST)

For target lesions

- Choose up to 5 lesions, up to 2 per organ
- Add up longest diameters (LD) of non-nodal lesions (axial plane)
- Add short axis diameters of nodes
- This is the "sum of the longest diameters" (SLD)

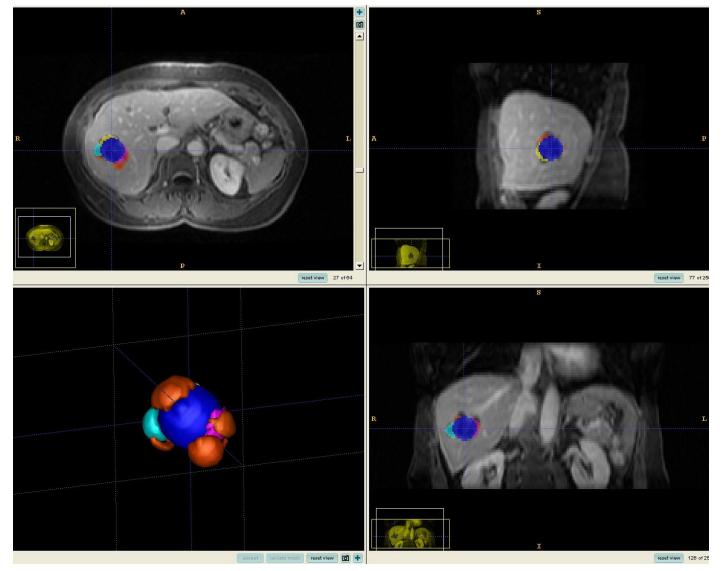
Response	Definition		
Complete Response (CR)	Disappearance of all extranodal target lesions. All pathological lymph nodes must have decreased to <10 mm in short axis.		
Partial Response (PR)	At least a 30% decrease in the SLD of target lesions, taking as reference the baseline sum diameters		
Progressive Disease (PD)	SLD increased by at least 20% from the smallest value on study (including baseline, if that is the smallest) The SLD must also demonstrate an absolute increase of at least 5 mm. (Two lesions increasing from 2 mm to 3 mm, for example, does not qualify)		
Stable Disease (SD)	Neither sufficient shrinkage to qualify for PR nor sufficient increase to qualify for PD		

(Liver) tumour shape pre-chemotherapy



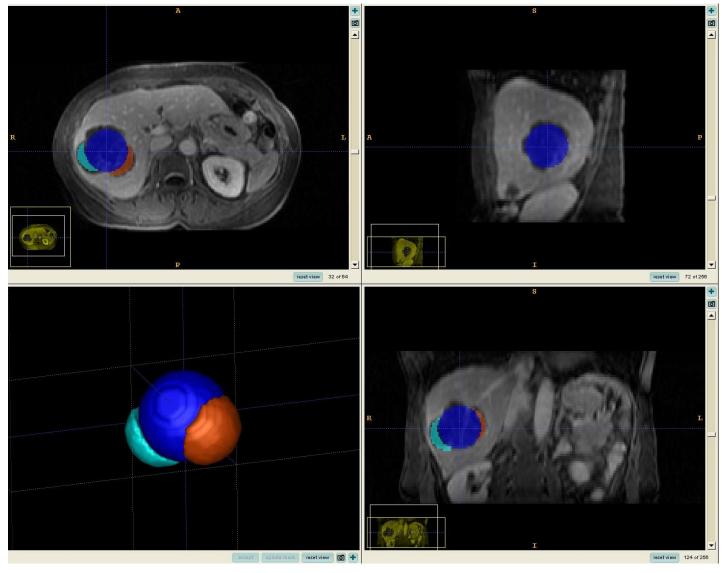
Eng Sci, Surgery, Radiology, Pathology, Clin Pharm, Mathematics, WIMM, GE Healthcare

Liver tumour shape post-chemotherapy, 9 months later



Eng Sci, Surgery, Radiology, Pathology, Clin Pharm, Mathematics, WIMM, GE Healthcare

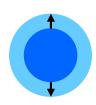
pre-ablation, another 3 months later

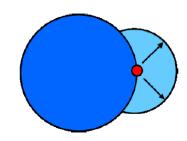


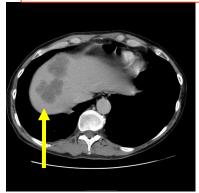
Eng Sci, Surgery, Radiology, Pathology, Clin Pharm, Mathematics, WIMM, GE Healthcare

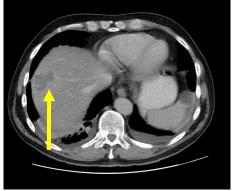
Tumour Growth Model

- Early tumour masses are often approximately spherical and grow as spheres. Mathematical models treat this case.
- They can sprout additional spheres (this corresponds, biologically, to clonal expansion)
- Heterogeneous tumours with multiple clonal centres may demonstrate variations in response to therapy (i.e. resistant clones)
- Can we relate morphological changes, determined from images, to underlying cancer growth processes?

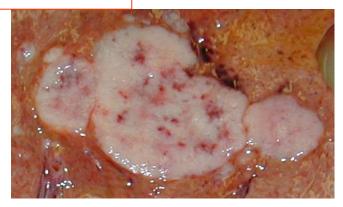










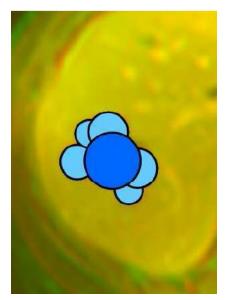


The shape of the resected specimen

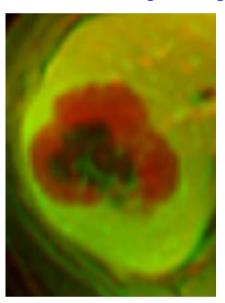
We conjecture that shape and shape changes encode the evolution, mutations, and severity of a tumour

Tumour growth model

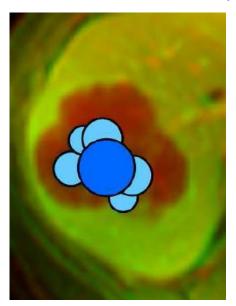
Clinical case from Churchill: growing metastatic colorectal (Dukes B) tumour



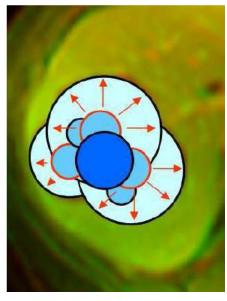
Spheroid fit after 9 months of chemotherapy



Tumour shape after 3 more months



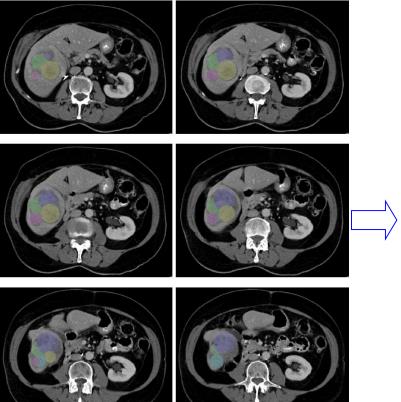
9 month spheroids centred on 12 month shape



9 month spheroids grown (red) and static/shrunk (black)

The tumour growth model gives a plausible account of tumour morphology; but the key question remains: do the successively sprouted clonal centres correspond to increasingly severe mutations of the original tumour DNA?

More precisely, we conjecture that the genomes of samples within a spheroid will show minor variation; but that the genomes of samples from different spheroids will have substantial variation.



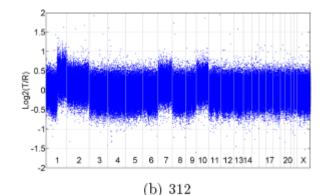
Sar	npleID	spheroid	labelling yield $[\mu g]$
	310	red	11.891
\	311	yellow	27.331
	312	torquoise	13.113
_/	313	torquoise	9.001
V	316Q	magenta	24.346
	317	magenta	24.91
	318	blue	10.27
	319	blue	9.729
	319	blue	9.72

3D model of tumour

DNA extraction (proteinase K digestion & purification).

Nuffield Department of Clinical Laboratory Sciences

Pre-resection CT (6 slices shown)



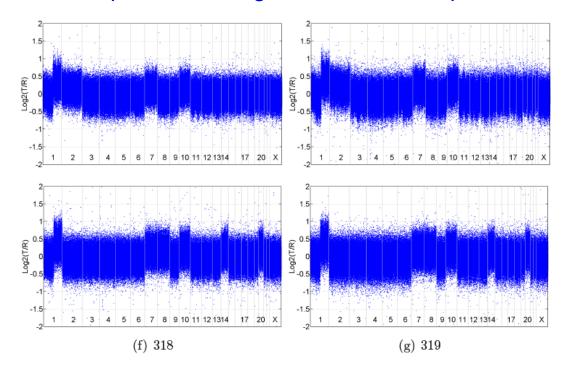
array Comparative Genomic Hybridization (aCGH), NimbleGen, Iceland

385,000 probes of a sample 17.4mm X 13mm → 6270 base pairs analysed

This shows the amplification of each of the genes in each of the chromosomes of the particular DNA sample – in this case from the turquoise spheroid

Log2 intensity ratios as a function of chromosome position for 7 hybridisations.

Horizontal axis is chromosome number; vertical axis is log intensity ratio – higher values show amplification of a particular chromosome = significant changes of the DNA sequence in the genes that make up the chromosome.



312 and 313 are from the same spheroid, and show *similar* amplification of chromosomes 2, 7, 10

318, 319 are both from another spheroid and show *similar* amplification of chromosomes 7, 8, 10, 14, and 20

More importantly, note that the amplification pattern is *different* for the two spheroids – this finding is repeated for *all distinct spheroids*.

We have linked developing tumour shape to increasing DNA mutations

So what?

Current clinical practice assesses tumour response to therapy using RECIST – Response Evaluation Criteria in Solid Tumours.

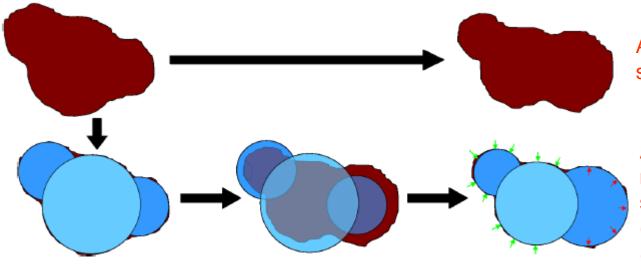
Disease *progression* ≡ increase by at least 20% in *longest linear dimension*

Disease *response* ≡ decrease by at least 30% in *longest linear dimension*

Otherwise, disease is considered to be stable

9 month tumour shape

12 month tumour shape



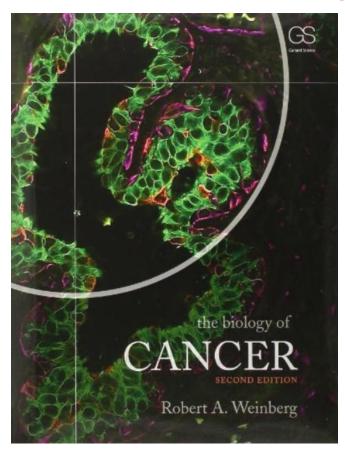
According to RECIST, stable disease

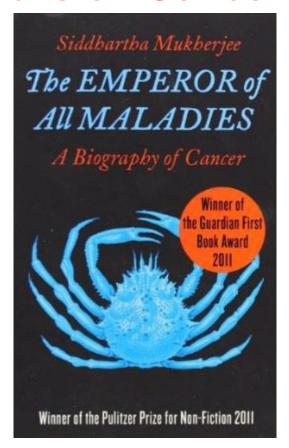
According to our model, the tumour has shown some response (green) but there is evidence of aggressive growth in a new spheroid

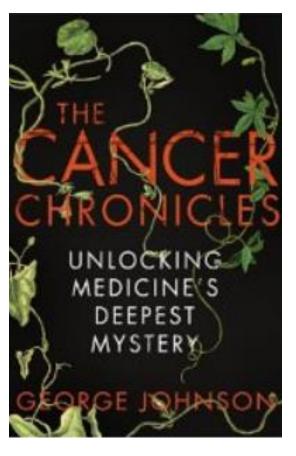
Conclusions

- Medical image analysis involves difficult image analysis challenges
- Doctors need numbers, error bars, results that enable them to do their jobs better
- Doctors couldn't care less about mathematics or algorithms, just results
- Models enable measurements in mammography, breast MRI, colorectal MRI, angiogenesis, and clonal expansion of tumours
- Measurements can also be misleading

Books on Cancer







Great introduction to cancer biology. Updated in 2013.

Wonderful popular history of cancer. Well worth buying.

A recent book, very well written, intermediate between the other two.